

$$MW = \text{MolarMass}(N_2)$$

"Inputs"

$$P\_tpsi = 300$$

$$P\_t = P\_tpsi * \text{convert}(\text{psi}, \text{psf})$$

$$V\_tgal = 3$$

$$V\_t = V\_tgal * \text{convert}(\text{gal}, \text{ft}^3)$$

$$T\_1 = 500$$

$$T\_1max = 560$$

$$P\_2 = 400$$

$$P\_1 = 2000$$

$$Rme = R * \text{convert}(\text{Btu/lbmol-R}, \text{ft-lbf/lbmol-R})$$

$$R\_g = Rme / MW$$

$$n = \text{IsentropicExponent}(N_2, T=T\_1)$$

"Isentropic expansion of nitrogen from P\_1 psi to P\_2 psi"

$$T\_2 = T\_1 * (P\_2/P\_1)^{(n-1)/n}$$

$$T\_g = (T\_2 + T\_1) / 2$$

$$W\_g = P\_t * V\_t / (R\_g * T\_g) \text{ "Net pressurant weight"}$$

"H&H procedure for sizing pressurant tanks"

"Compute pressurant volume"

"gross gas requirement = net system pressurant requirement + residual gas in storage vessel"

$$P\_1 * \text{convert}(\text{psi}, \text{psf}) * V\_L / (T\_1 * R\_g) = W\_g + P\_2 * \text{convert}(\text{psi}, \text{psf}) * V\_L / (T\_2 * R\_g)$$

"Compute gross pressurant weight - include 2% margin"

$$W\_p = P\_1 * \text{convert}(\text{psi}, \text{psf}) * V\_L / (R\_g * T\_1) * 1.02$$

"Compute required volume of the storage vessel"

$$V\_u = R\_g * T\_1max * W\_p / (P\_1 * \text{convert}(\text{psi}, \text{psf}))$$

$$V\_ugal = V\_u * \text{convert}(\text{ft}^3, \text{gal})$$

"Sutton procedure for sizing pressurant tanks"

$$P\_p = P\_t$$

$$V\_p = V\_t$$

$$k = n$$

$$T\_0 = T\_1$$

$$P\_g = P\_2 * \text{convert}(\text{psi}, \text{psf})$$

$$P\_0 = P\_1 * \text{convert}(\text{psi}, \text{psf})$$

$$m\_0 = P\_p * V\_p * k / (R\_g * T\_0 * (1 - P\_g / P\_0))$$

$$V\_0 = m\_0 * R\_g * T\_0 / P\_0$$

$$V\_0gal = V\_0 * \text{convert}(\text{ft}^3, \text{gal})$$

SOLUTION

**Unit Settings: Eng R psia mass deg**

$$k = 1.4$$

$$MW = 28.01 \text{ [lbm/lbmol]}$$

$$m_0 = 1.1 \text{ [lbm]}$$

$$n = 1.4$$

$$P_0 = 287998 \text{ [psf]}$$

$$P_1 = 2000 \text{ [psia]}$$

$$P_2 = 400 \text{ [psia]}$$

$$P_g = 57600 \text{ [psf]}$$

$$P_p = 43200 \text{ [psf]}$$

$$P_t = 43200 \text{ [psf]}$$

$$P_{\text{tpsi}} = 300 \text{ [psi]}$$

$$R_{\text{me}} = 1545 \text{ [ft-lbf/lbmol-R]}$$

$$R_g = 55.16 \text{ [ft-lbf/lbm-R]}$$

$$T_0 = 500 \text{ [R]}$$

$$T_1 = 500 \text{ [R]}$$

$$T_{1\text{max}} = 560 \text{ [R]}$$

$$T_2 = 315.6 \text{ [R]}$$

$$T_g = 407.8 \text{ [R]}$$

$$V_0 = 0.1053 \text{ [ft}^3\text{]}$$

$$V_{0\text{gal}} = 0.7878 \text{ [gal]}$$

$$V_L = 0.108 \text{ [ft}^3\text{]}$$

$$V_p = 0.401 \text{ [ft}^3\text{]}$$

$$V_t = 0.401 \text{ [ft}^3\text{]}$$

$$V_{\text{tgal}} = 3 \text{ [gal]}$$

$$V_u = 0.1234 \text{ [ft}^3\text{]}$$

$$V_{\text{ugal}} = 0.9228 \text{ [gal]}$$

$$W_g = 0.7702 \text{ [lbm]}$$

$$W_p = 1.15 \text{ [lbm]}$$

No unit problems were detected.